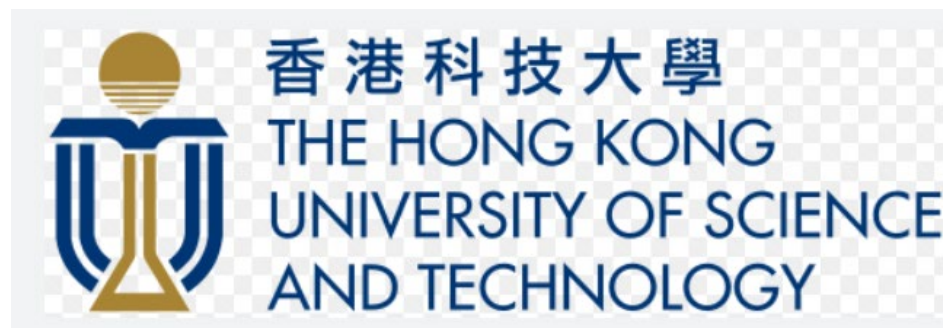




LHMM: A Learning Enhanced HMM Model for Cellular Trajectory Map Matching

Weijie Shi, Jiajie Xu*, Junhua Fang, Pingfu Chao, An Liu, and Xiaofang Zhou



Two Basic Concepts

Cellular Data



Cell tower



Carrier Server

UserID	Timestamp	Cell towerID
A01	0802081032	37146
A01	0802081046	37149
A01	0802081068	37150
A01	0802081103	37153
A01	0802081148	37121
A01	0802081182	37154

.....

Two Basic Concepts

Cellular Trajectory Map-Matching



● GPS trajectory point

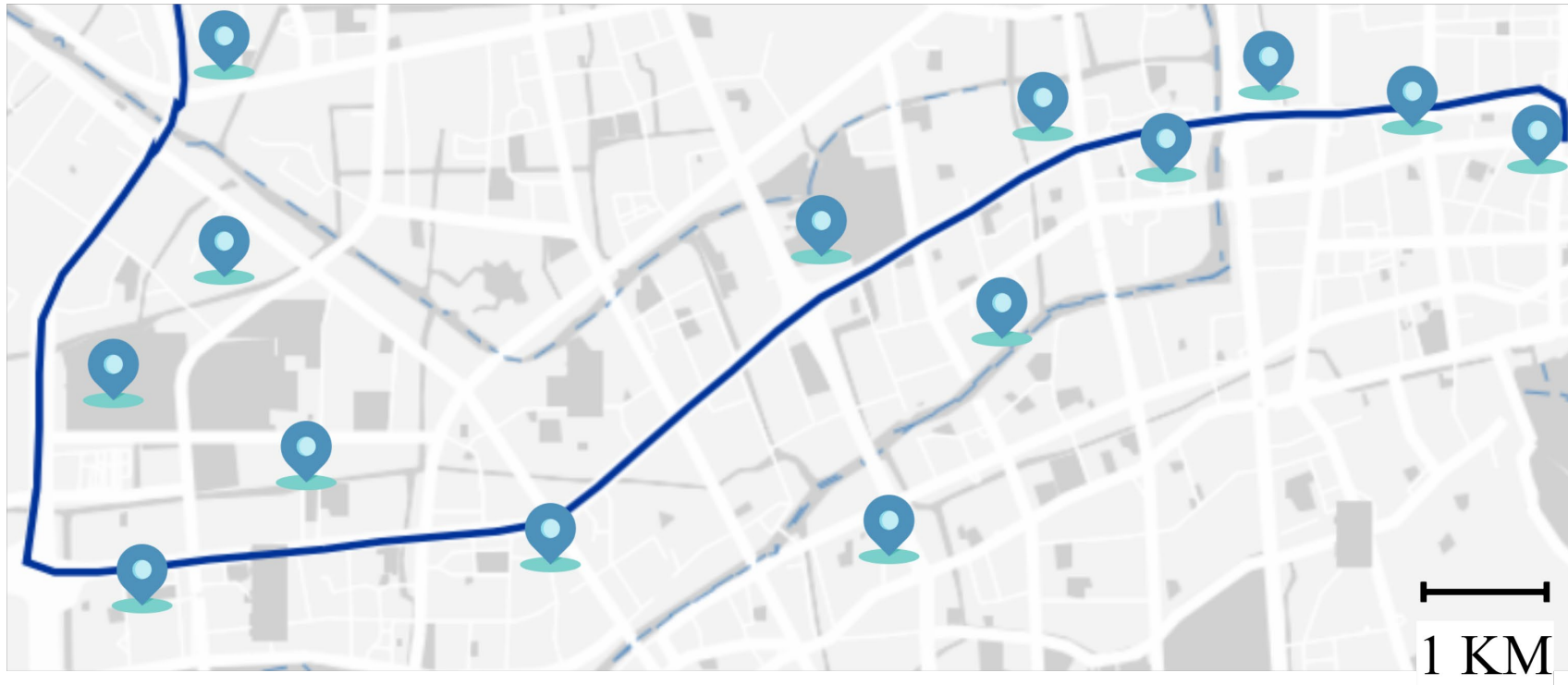


cellular trajectory point

— traveled path

Two Basic Concepts

Cellular Trajectory Map-Matching

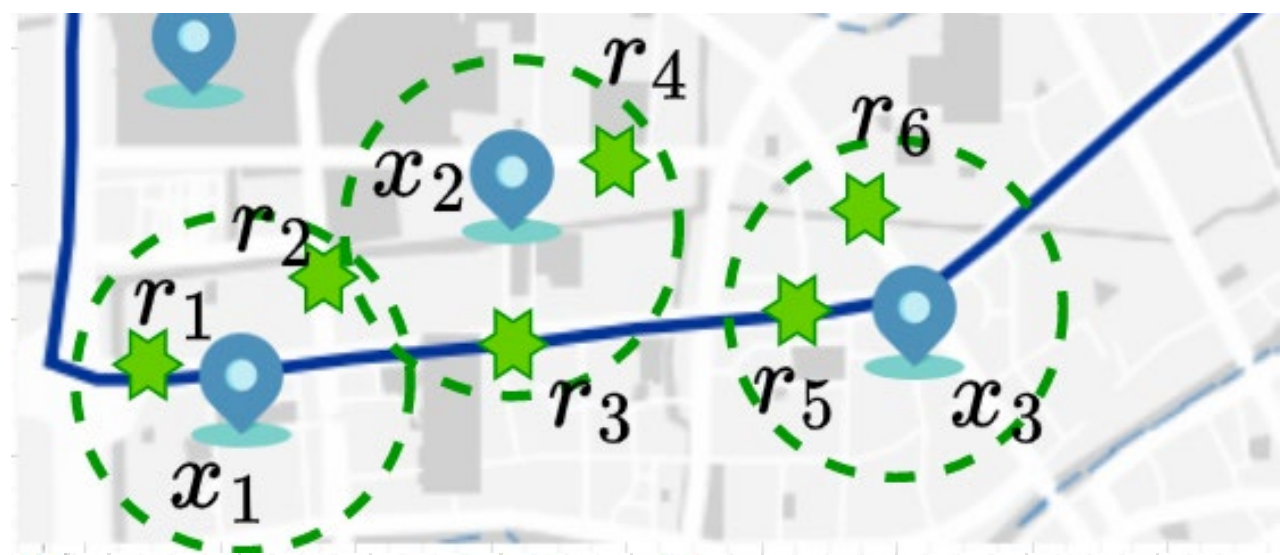


● GPS trajectory point 📍 cellular trajectory point — traveled path

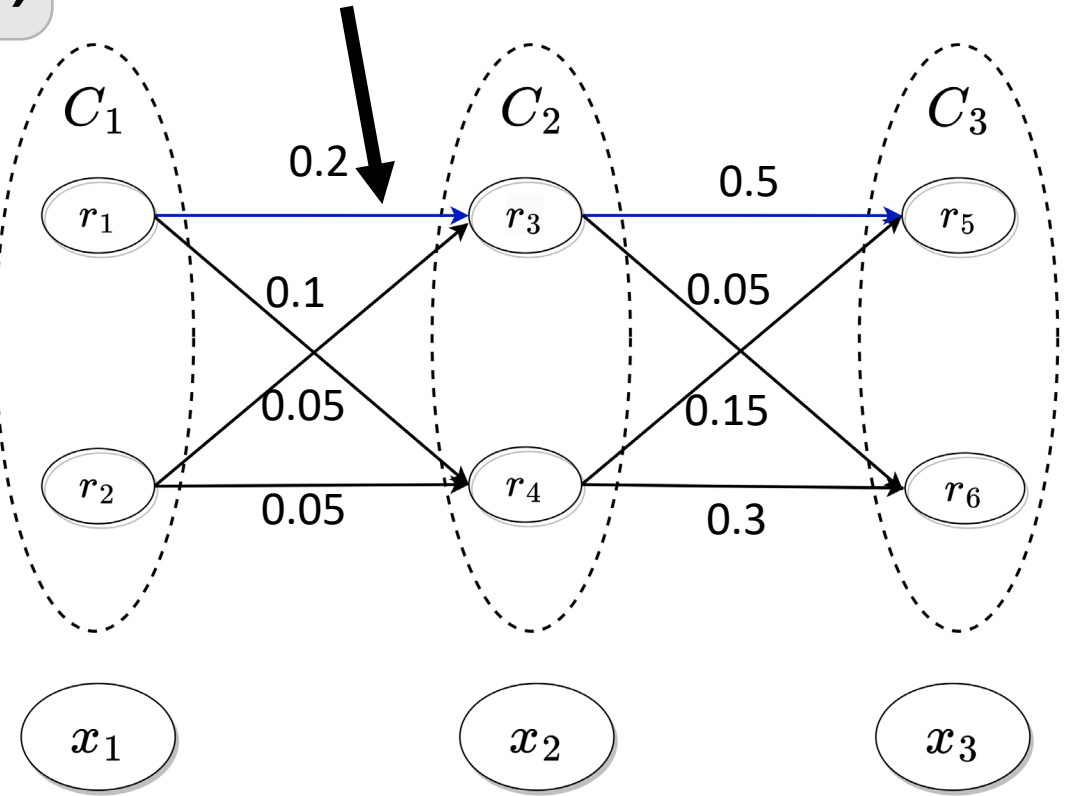
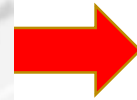
Existing Methods

Hidden Markov Model (HMM)

Observation Probability \times Transition Probability



HMM's candidate road segments for a point

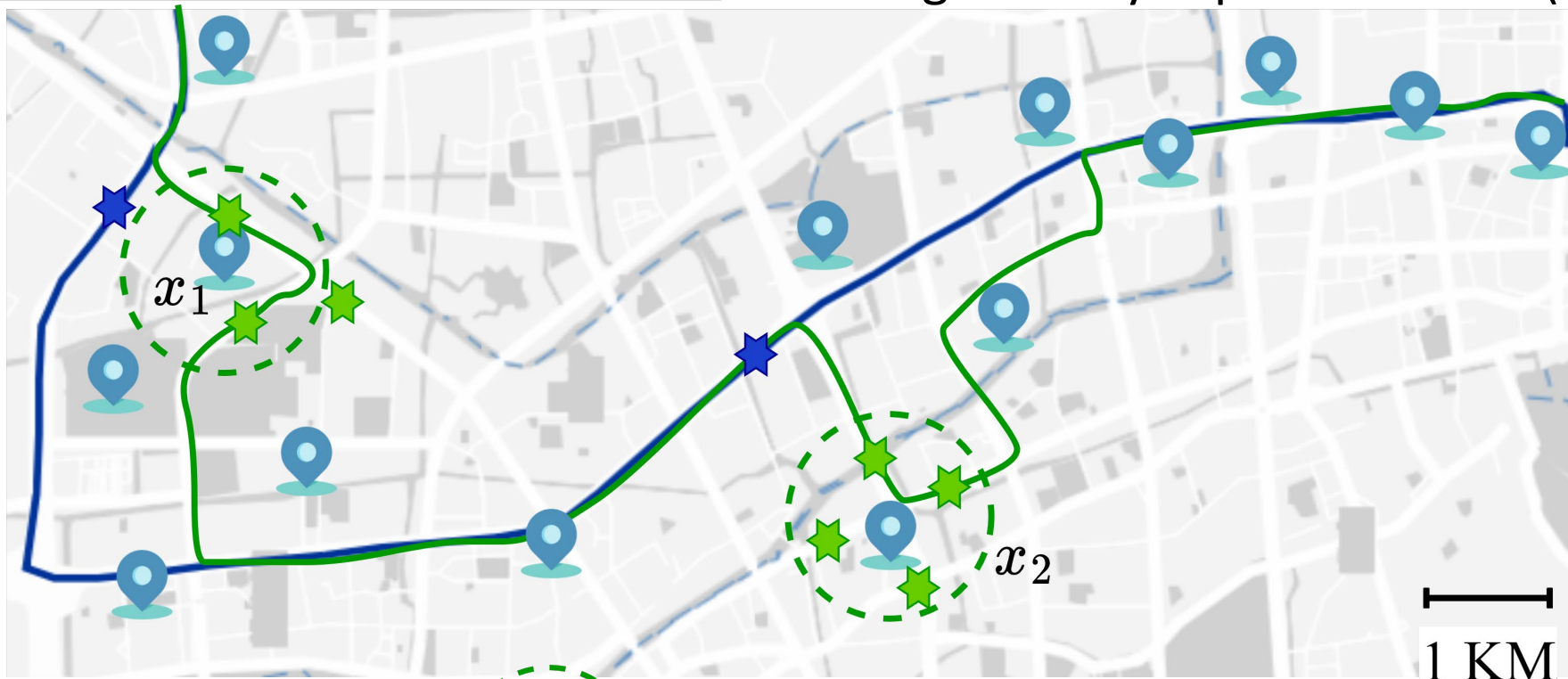


Lattice Graph

Existing Methods

HMM's Drawback

The observation probability P_O and transition probability P_T are guided by explicit features (like distance)



HMM-based model
matching result



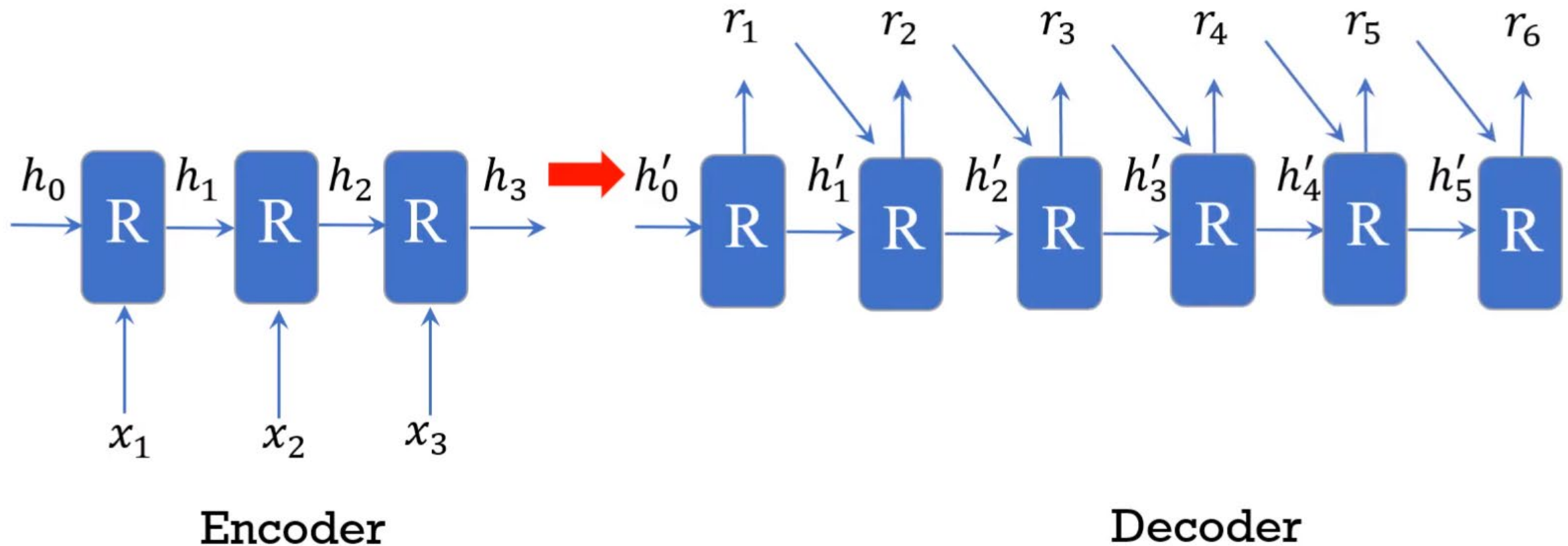
HMM's candidate road
segments for a point



traveled road segment

Existing Methods

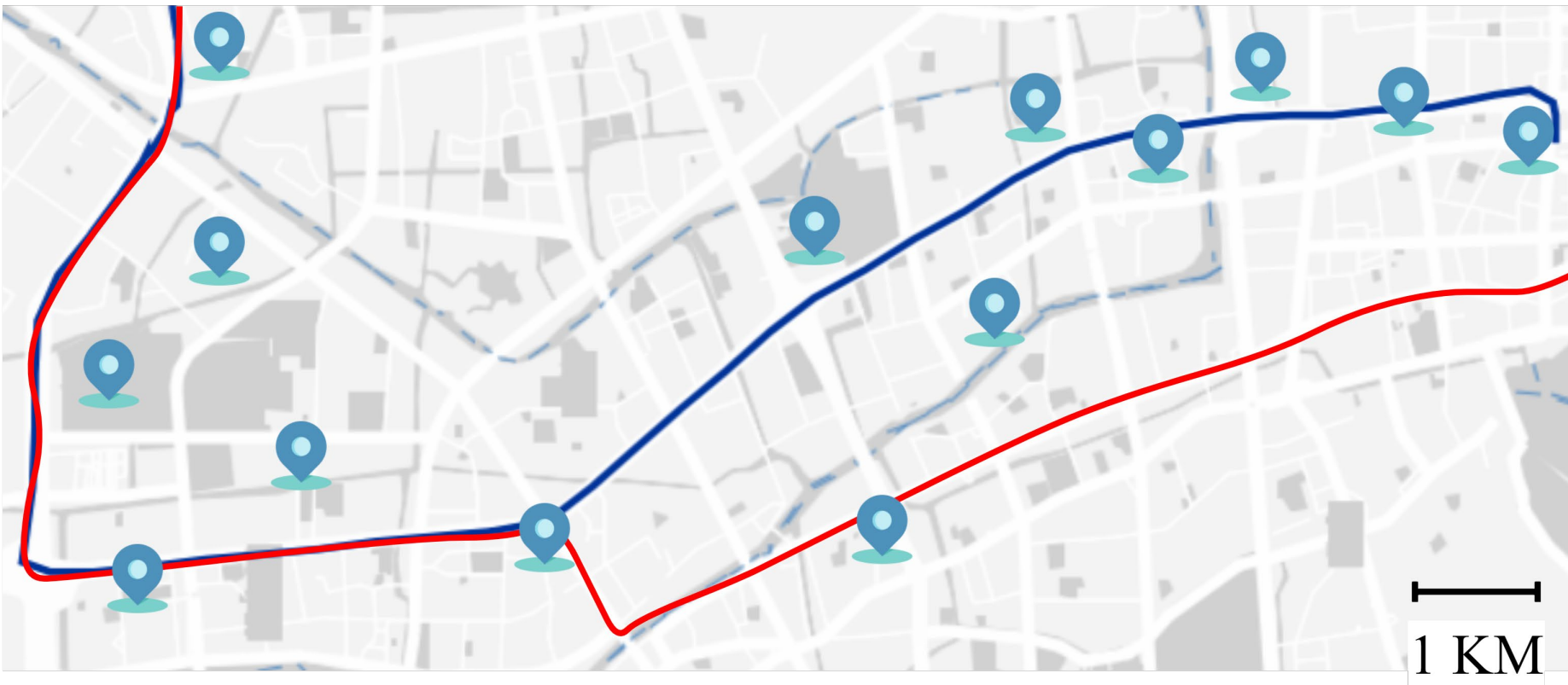
Sequence to Sequence Model (Seq2Seq)



Existing Methods

Seq2Seq's Drawback

Facing severe error propagation

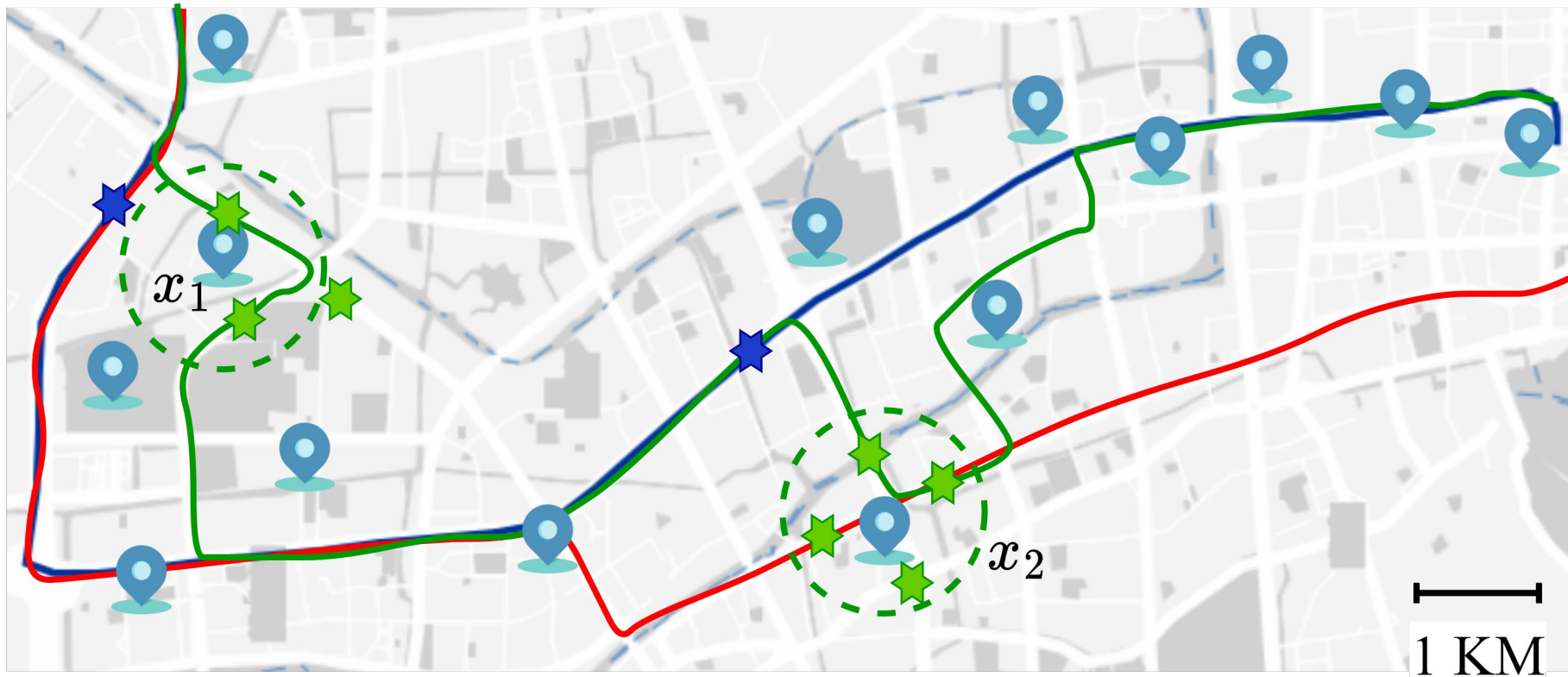


— Seq2seq-based model
matching result

— traveled path

Existing Methods

Advantages of HMM and Seq2Seq



— HMM-based model matching result — Seq2seq-based model matching result — traveled path

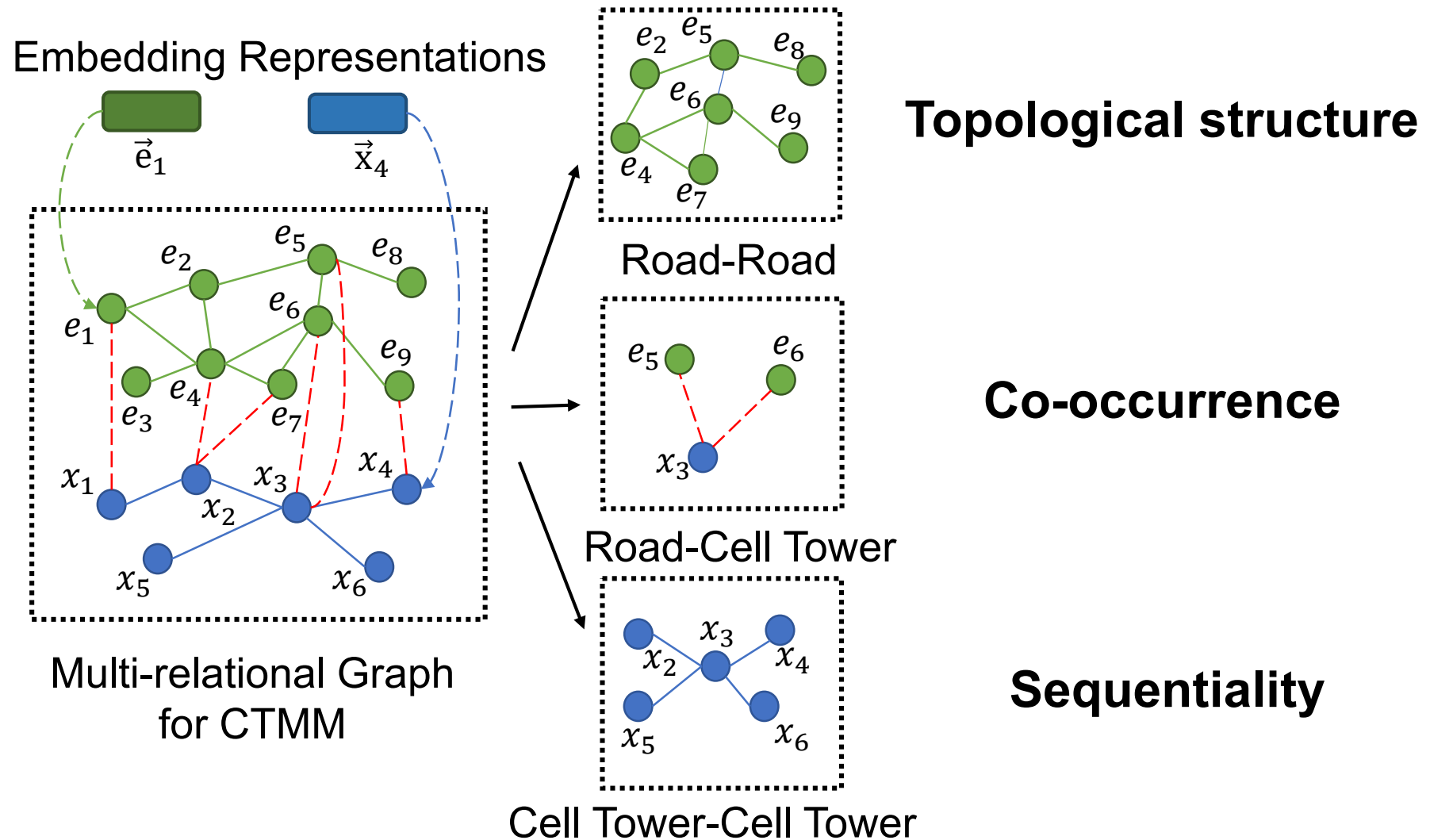
Learning Enhanced Hidden Markov Model

Learning Enhanced Hidden Markov Model

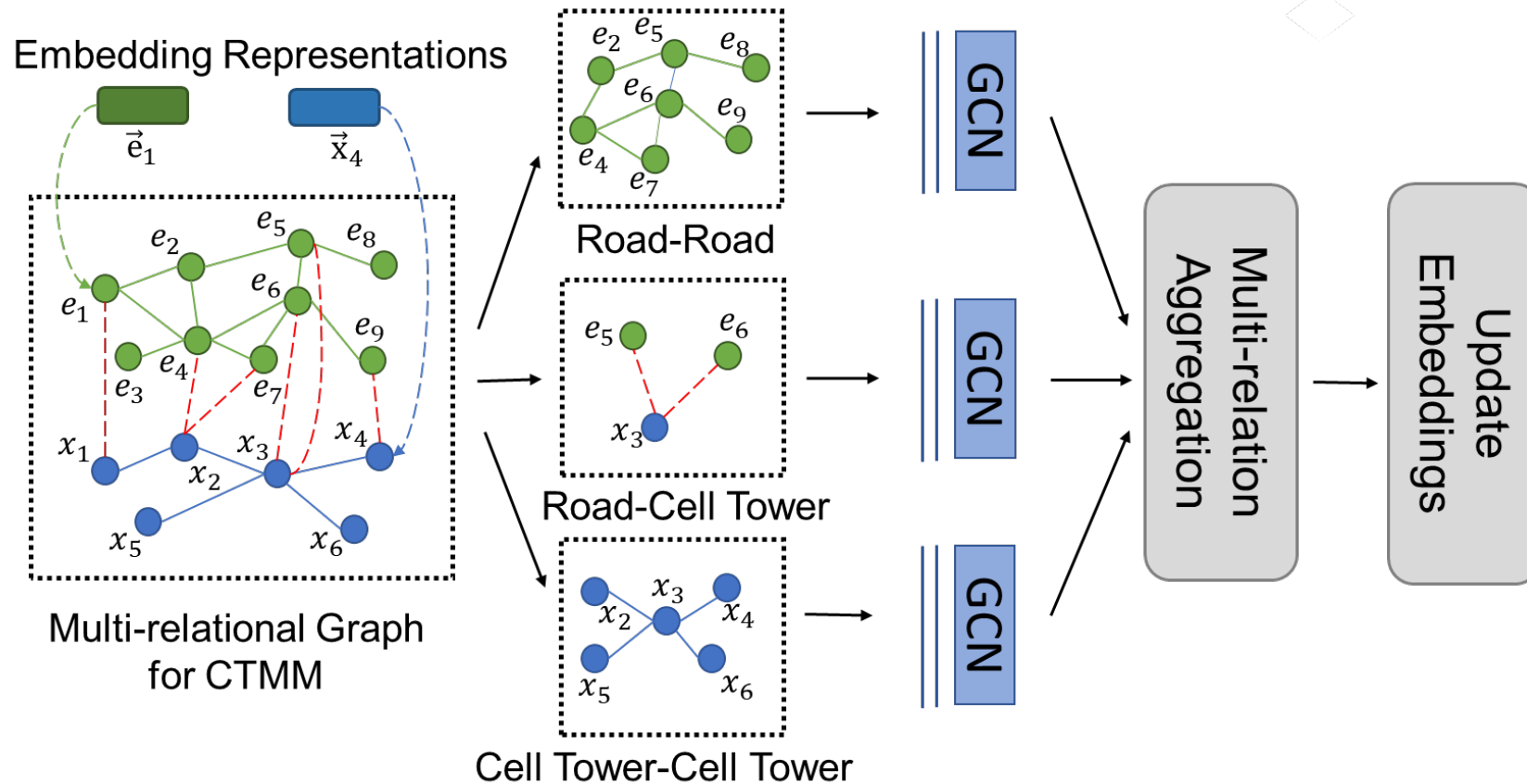
Aim to using **Neural Network** instead of hand-designed heuristic
to learn **Observation Probability P_O** and **Transition Probability P_T**

Challenge 1 – Multi-relation Representation Learning

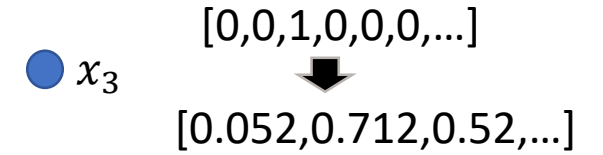
How to effectively capture these relations and embedded them into a shared space?



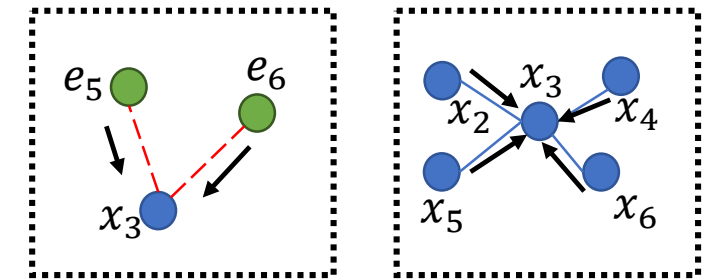
Solution 1 – Multi-relation Representation Learning



Step1: Initialize



Step2: Message passing



$$z_i^{rel} = \frac{1}{|\mathcal{N}_i^{rel}|} \sum_{v_j \in \mathcal{N}_i^{rel}} W_{rel}^{(l)} h_j^{(l)}$$

Step3: jointly aggregate the message
And update the

$$h_i^{(l+1)} = \sigma \left(\sum_{rel \in \mathcal{R}} W_{agg} z_i^{rel} + W_0^{(l)} h_i^{(l)} \right)$$

Challenge 2 – Learning for Observation Probability

For P_O : there are too roads with high relevant with the point x_2



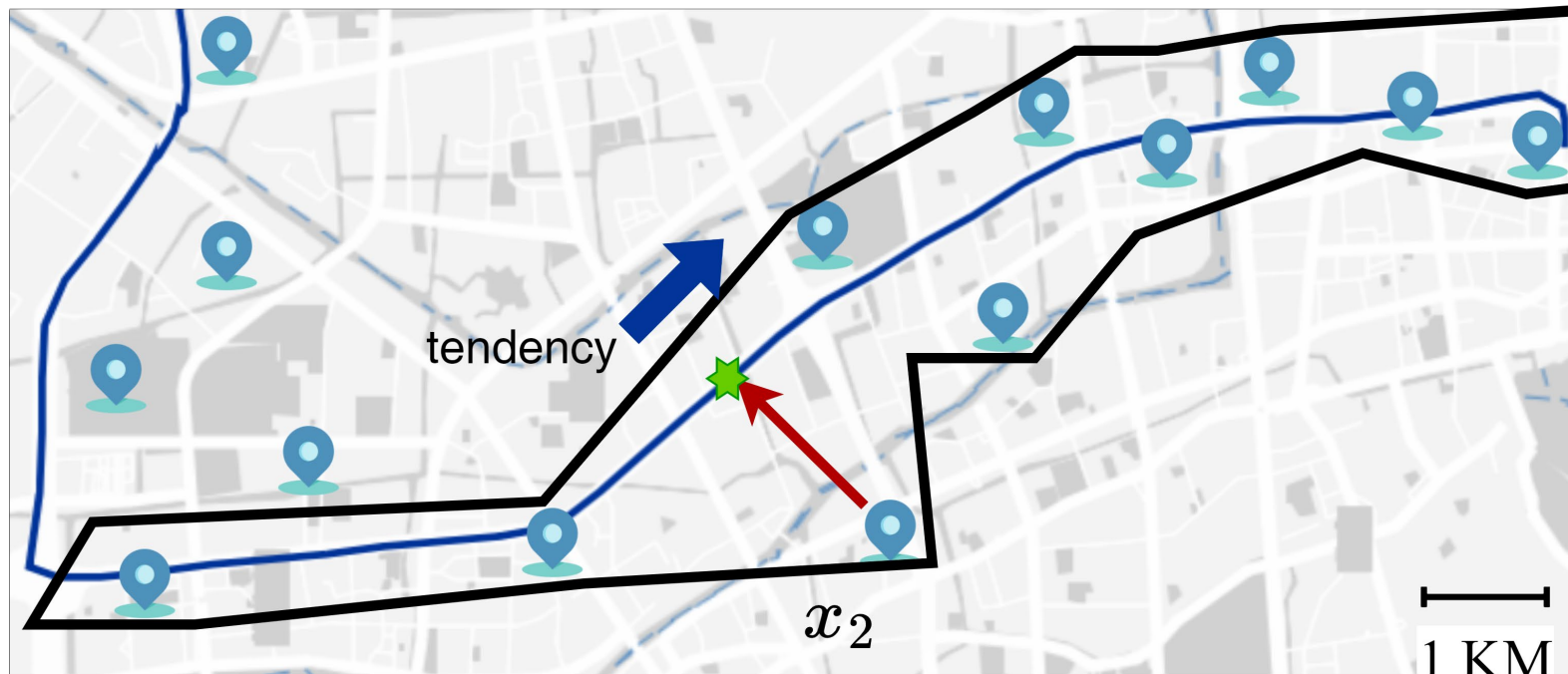
cellular trajectory point



traveled path

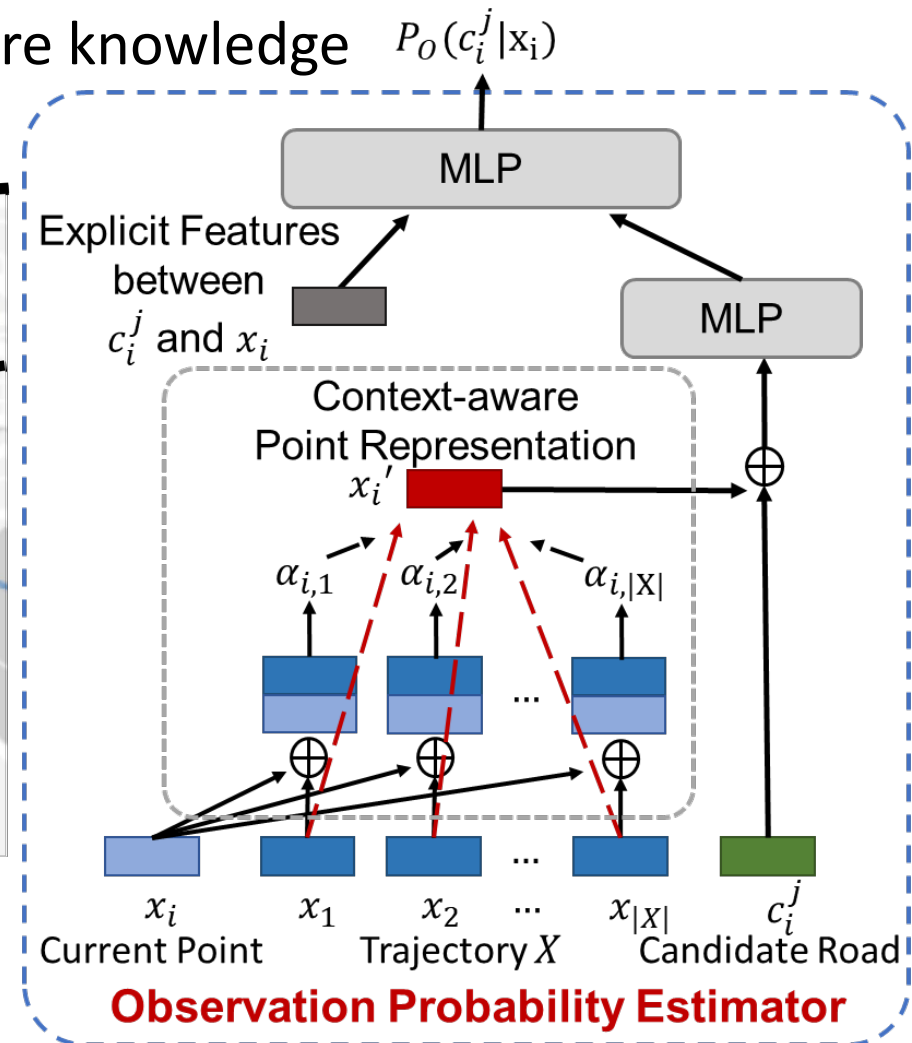
Solution 2 – Learning for Observation Probability

For P_o : capture the implicit point-road with context-aware knowledge $P_o(c_i^j | x_i)$



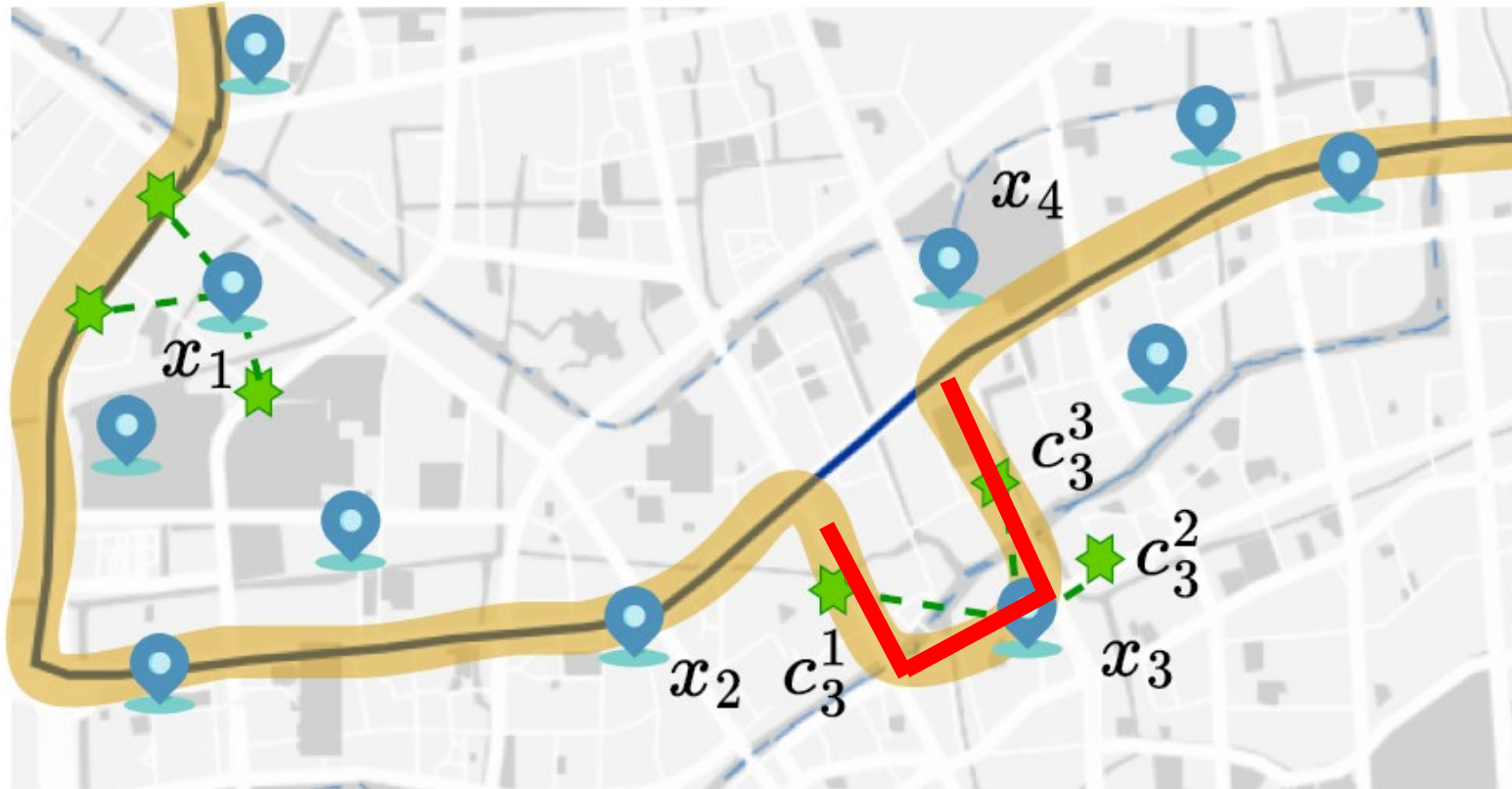
cellular trajectory point


traveled path



Challenge 3 – Learning for Transition Probability

For P_T : how to test the detour of the moving path?




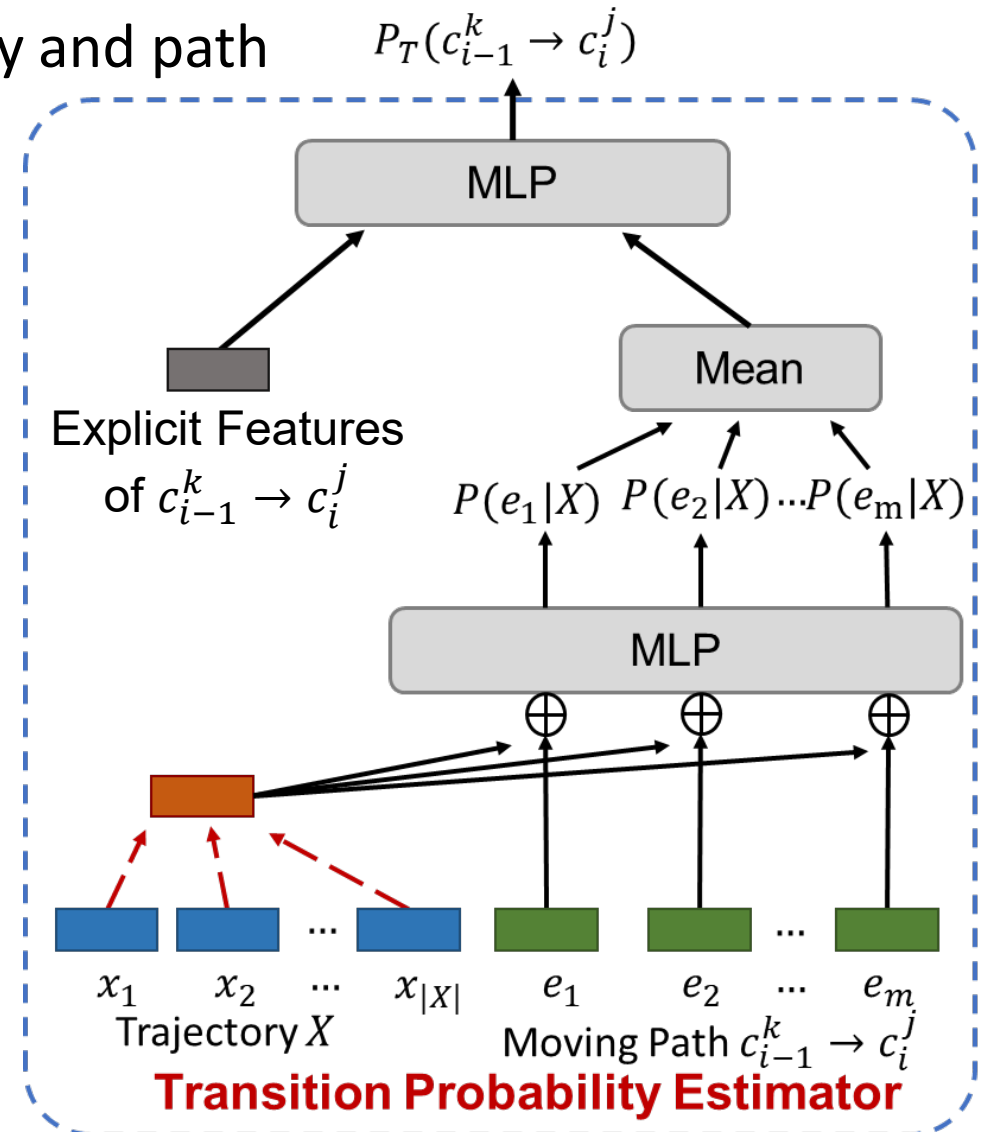
 matching result

Solution 3 – Learning for Transition Probability

For P_T : capture the implicit features between trajectory and path

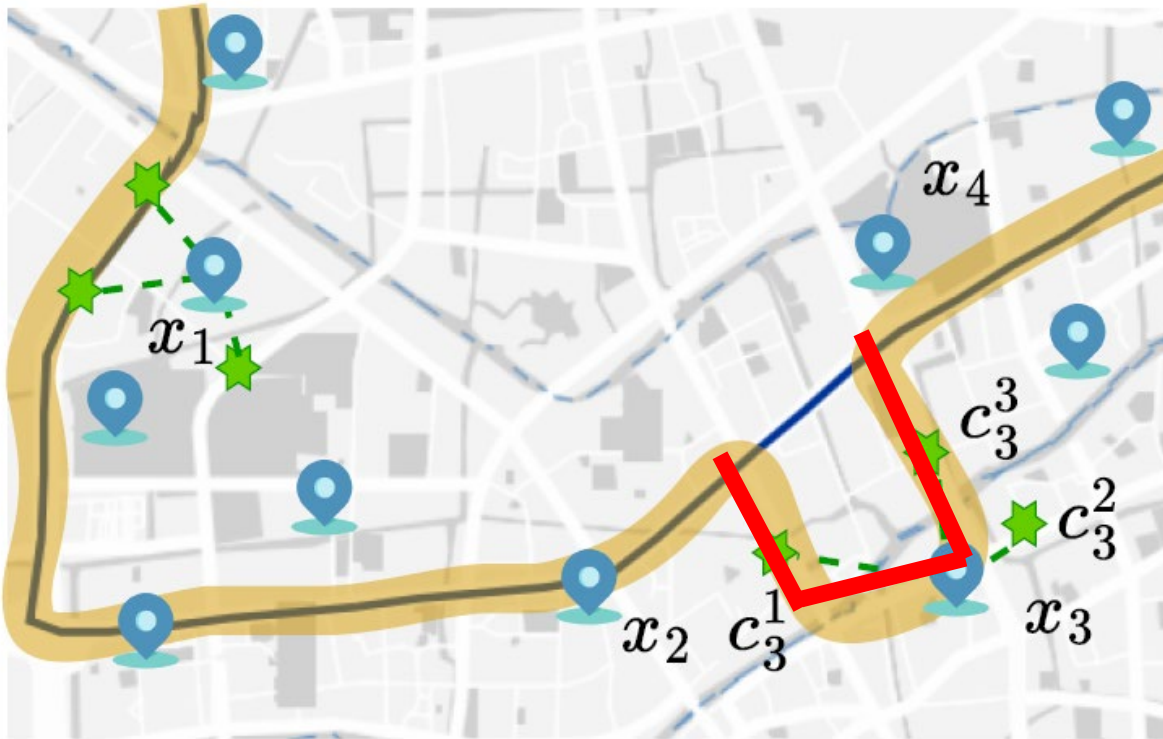



 matching result

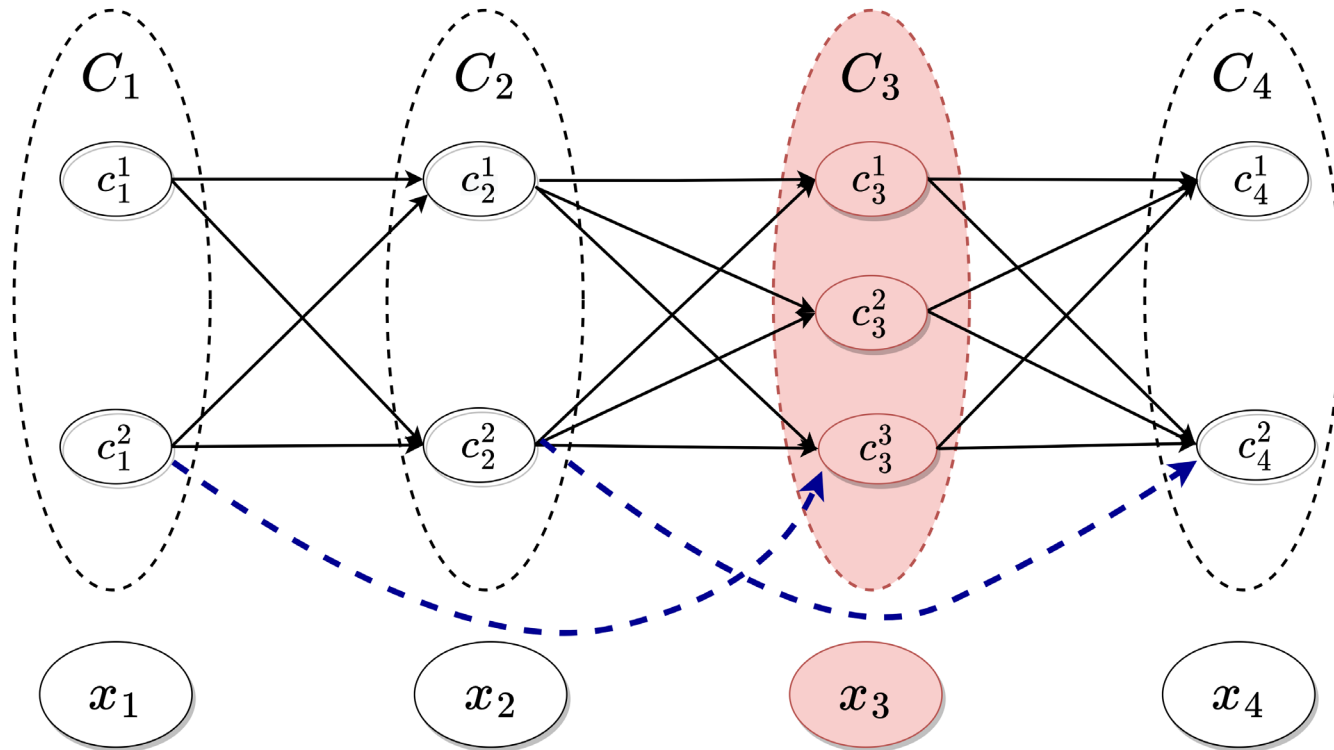


Challenge 4 – Improved Lattice Graph

how to remedy the detour of the moving path?

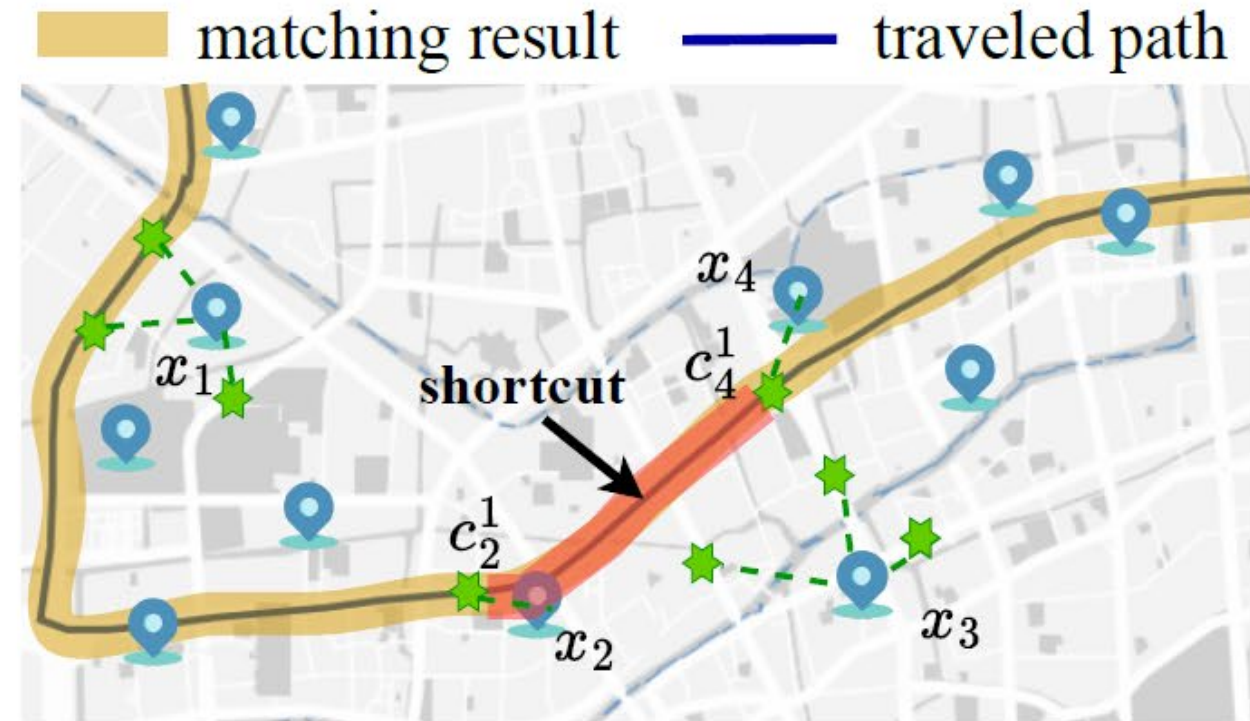
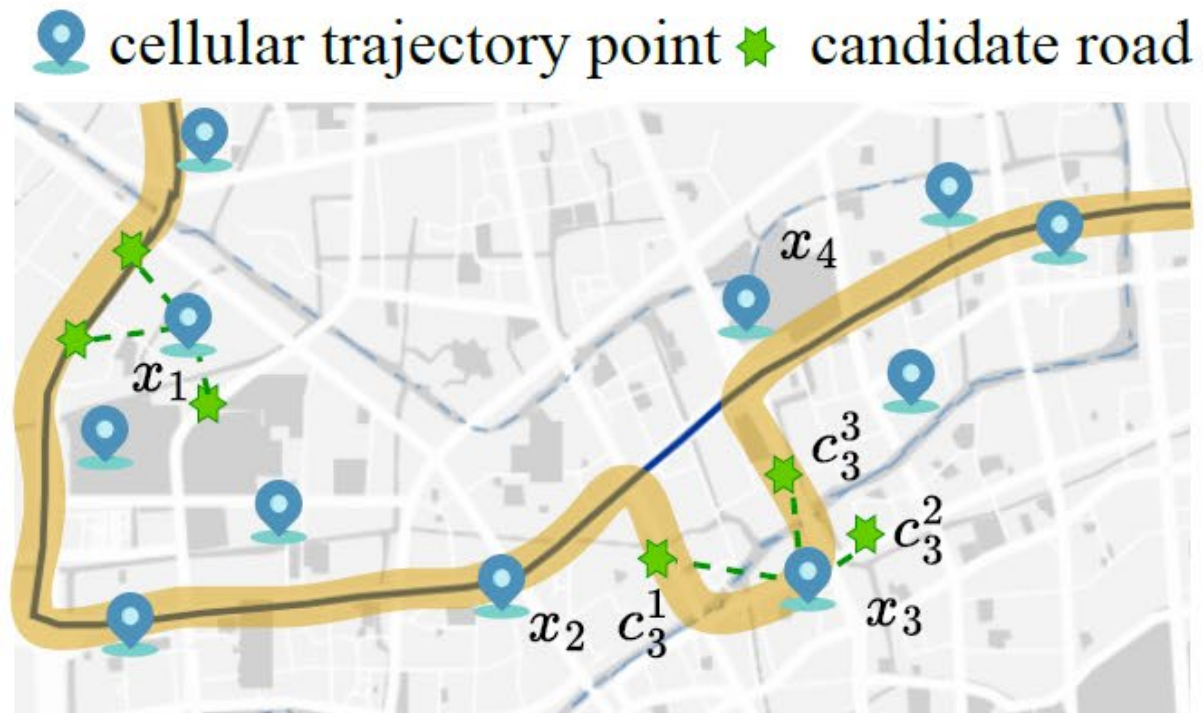


 matching result



Solution 4 – Improved Lattice Graph

using shortcuts to provide chances to skip the unqualified candidate set



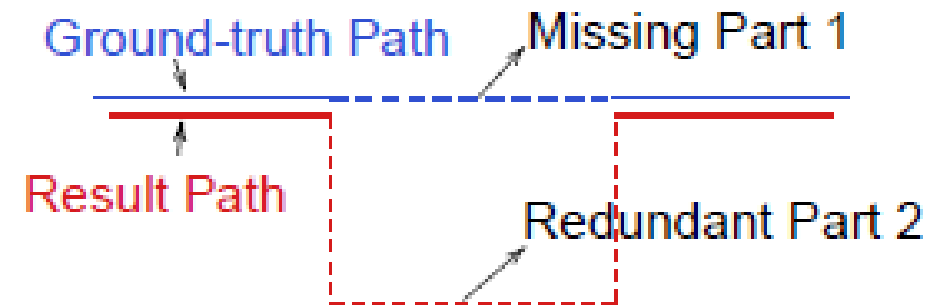
Experiment - Dataset

category	Hangzhou	Xiamen
road segments	92,913	64,828
intersections	67,330	37,591
all cellular trajectory points	3.61 million	1.18 million
all GPS trajectory points	9.73 million	4.98 million
cellular trajectory points per trajectory	34	40
GPS trajectory points per trajectory	81	88
average cellular sampling interval (s)	67	42
maximum cellular sampling interval (s)	247	185
average cellular sampling distance (m)	730	650
median cellular sampling distance (m)	493	455

DATASET CHARACTERISTIC

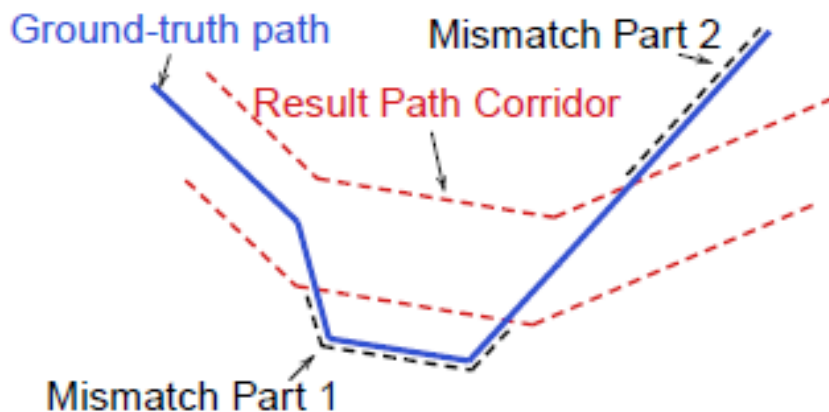
Experiment - Evaluation criteria

- Precision and Recall
- Route Mismatch Fraction (RMF)
- Corridor Mismatch Fraction (CMF)



RMF

$$\text{RMF} = \frac{\sum \text{length of mismatched road segments}}{\text{length of the ground-truth path}}$$



CMF

$$\text{CMF} = \frac{\sum \text{corridor uncovered length}}{\text{length of the ground-truth path}}$$

Experiment - Evaluation criteria

- Precision and Recall
- Route Mismatch Fraction (RMF)
- Corridor Mismatch Fraction (CMF)
- Hitting Ratio (HR)
- Average inference Time (Avg Time)



HMM's candidate road segments for a point

Experiment – Overall Performance

HMM based methods

Dataset Metric	Hangzhou					Xiamen				
	Precision	Recall	RMF	CMF50	Avg Time (s)	Precision	Recall	RMF	CMF50	Avg Time (s)
Methods designed for GPS trajectory map-matching										
STM [8]	0.388	0.476	1.237	0.225	0.040	0.411	0.498	1.050	0.198	0.044
IVMM [10]	0.409	0.518	1.125	0.188	0.101	0.428	0.529	0.936	0.172	0.136
IEM [32]	0.430	0.522	1.024	0.178	0.045	0.451	0.537	0.889	0.167	0.048
DeepMM [37]	0.446	0.544	0.881	0.172	0.951	0.478	0.568	0.785	0.158	1.284
MCM [34]	0.449	0.552	0.893	0.169	0.033	0.479	0.572	0.780	0.152	0.039
TransformerMM [38]	0.455	0.552	0.838	0.170	1.667	0.483	0.577	0.769	0.153	1.857
Methods designed for CTMM										
CLSTERS [41]	0.443	0.551	0.922	0.173	0.043	0.470	0.563	0.805	0.154	0.048
SNet [12]	0.446	0.555	0.891	0.169	0.034	0.475	0.565	0.792	0.153	0.041
THMM [42]	0.461	0.562	0.815	0.165	0.041	0.486	0.583	0.767	0.148	0.045
DMM [15]	0.467	0.566	0.784	0.163	0.853	0.489	0.594	0.755	0.145	0.916
Our method										
LHMM	0.516	0.613	0.670	0.126	0.032	0.547	0.667	0.641	0.124	0.037
Improved	10.49%	8.30%	14.54%	22.69%	3.03%	11.86%	12.28%	8.79%	15.09%	5.12%

Seq2Seq based methods

Experiment – Ablation Results

Dataset	Variant	Precision	CMF50	HR
Hangzhou	LHMM	0.516	0.126	0.953
	LHMM-E	0.457	0.142	0.931
	LHMM-H	0.489	0.136	0.942
	LHMM-O	0.428	0.178	0.920
	LHMM-T	0.472	0.155	0.926
	LHMM-S	0.484	0.140	0.937
	STM	0.388	0.225	0.874
	STM+S	0.405	0.189	0.911
Xiamen	LHMM	0.545	0.125	0.965
	LHMM-E	0.494	0.144	0.938
	LHMM-H	0.517	0.142	0.942
	LHMM-O	0.462	0.158	0.931
	LHMM-T	0.524	0.135	0.952
	LHMM-S	0.516	0.139	0.944
	STM	0.411	0.198	0.882
	STM+S	0.432	0.170	0.915

Experiment – Ablation Results

Dataset	Variant	Precision	CMF50	HR
Hangzhou	LHMM	0.516	0.126	0.953
	LHMM-E	0.457	0.142	0.931
	LHMM-H	0.489	0.136	0.942
	LHMM-O	0.428	0.178	0.920
	LHMM-T	0.472	0.155	0.926
	LHMM-S	0.484	0.140	0.937
	STM	0.388	0.225	0.874
	STM+S	0.405	0.189	0.911
Xiamen	LHMM	0.545	0.125	0.965
	LHMM-E	0.494	0.144	0.938
	LHMM-H	0.517	0.142	0.942
	LHMM-O	0.462	0.158	0.931
	LHMM-T	0.524	0.135	0.952
	LHMM-S	0.516	0.139	0.944
	STM	0.411	0.198	0.882
	STM+S	0.432	0.170	0.915

Experiment – Ablation Results

Dataset	Variant	Precision	CMF50	HR
Hangzhou	LHMM	0.516	0.126	0.953
	LHMM-E	0.457	0.142	0.931
	LHMM-H	0.489	0.136	0.942
	LHMM-O	0.428	0.178	0.920
	LHMM-T	0.472	0.155	0.926
	LHMM-S	0.484	0.140	0.937
	STM	0.388	0.225	0.874
	STM+S	0.405	0.189	0.911
Xiamen	LHMM	0.545	0.125	0.965
	LHMM-E	0.494	0.144	0.938
	LHMM-H	0.517	0.142	0.942
	LHMM-O	0.462	0.158	0.931
	LHMM-T	0.524	0.135	0.952
	LHMM-S	0.516	0.139	0.944
	STM	0.411	0.198	0.882
	STM+S	0.432	0.170	0.915

Experiment – Ablation Results

Dataset	Variant	Precision	CMF50	HR
Hangzhou	LHMM	0.516	0.126	0.953
	LHMM-E	0.457	0.142	0.931
	LHMM-H	0.489	0.136	0.942
	LHMM-O	0.428	0.178	0.920
	LHMM-T	0.472	0.155	0.926
	LHMM-S	0.484	0.140	0.937
	STM	0.388	0.225	0.874
	STM+S	0.405	0.189	0.911
Xiamen	LHMM	0.545	0.125	0.965
	LHMM-E	0.494	0.144	0.938
	LHMM-H	0.517	0.142	0.942
	LHMM-O	0.462	0.158	0.931
	LHMM-T	0.524	0.135	0.952
	LHMM-S	0.516	0.139	0.944
	STM	0.411	0.198	0.882
	STM+S	0.432	0.170	0.915

Summary

- we have developed a learning-enhanced HMM map-matching approach for cellular trajectories.
- A representation learning component is designed to fully capture multi-relational information tailored for the CTMM task.
- A learned observation probability captures the implicit context-aware correlation between roads and points for better positioning denoising, and a learned transition probability models the hidden relevance between moving paths and trajectories.
- These two probabilities then guide the path-finding process on an improved candidate graph.